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Application of Duration Measure in Quantifying the Sensitivity of Project Returns to Changes in Discount Rates

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Abstract: In this research, the concept of Duration with a new application in project management has been defined. The Duration of each project provides the project manager with a combined measure containing concepts of return, cost and time of the project. Further in this article, the changes in project return, based on different assumptions such as discount rate, have been examined. To examine the effect of the changes in these factors, the Monte Carlo simulation has been used. The relationship between these factors is nonlinear which reflects the great importance of investment on appropriate risk management systems. The data from a set of construction projects have been used in order to verify the results of this study. Similar relationships can be expected to exist in other industries as well.

Keywords: project duration; convexity; discount rate risk; reinvestment risk; risk measures; monte carlo simulation

1. Introduction

The purpose of this study is to introduce a new concept in Project Management. Based on PMI definition, a project is a temporary endeavor undertaken to create a unique product, service, or result. There are various standards for proper management of the projects. PMI's A Guide to the Project Management Body of Knowledge (PMBOK® Guide) is one of the main project management standards. Based on this standard, Project management is the application of knowledge, skills, tools, and techniques to project activities in order to meet the project requirements. For this purpose, 10 knowledge areas are defined to properly manage the project tasks, which include: Integration, Scope, Scheduling, Cost, Quality, Procurement, Resources, Communications, Risk and Stakeholder management (Project Management Institute 2017). Different areas, such as time, cost, quality, etc. have been defined for efficient management of projects. The definition of these areas is often done separately. However, in practice all of these different areas affect each other and any decision that may have effects on any of them can lead to changes in other relevant areas. Many studies have been conducted on the effect of these areas, on each other. In this study, we have introduced a new concept known as the Duration. This title has sometimes been used, in different studies, for time management and with the purpose of scheduling. The concept addressed in our study has been covered to a great extent in the finance literature. In the discussions regarding bonds, this concept was first defined by Macaulay.

2. Project Duration

Duration is a well-established and practical concept in finance literature. The concept of duration was first introduced by Macaulay (1938). After duration was presented lots of studies were carried out on its usages. Weil (1973) in his research titled, Macaulay's duration: an appreciation, investigated the various applications of this practical measure. Boquist et al. (1975) used duration as a risk assessment tool. After that much research has been conducted on the concept of duration. Osborne (2005) developed a more precise formula for duration. Dierkes and Ortmann (2015) proposed an estimation model and compared it with approximation methods that were based on duration. Sarkar and Hong (2004) estimated the effective duration for corporate bonds with call provision. Jacoby and Roberts (2003) studied the adjustment of Macaulay duration caused by call and default. Xie et al. (2009) investigated the effect of these two factors on duration. Lee et al. (2011) investigated the effect of sovereign risk on duration. Hatchondo and Martinez (2009) investigated the possibility of government borrowing using long-duration bonds, and its impact on the level and volatility of interest rates. Bejaoui and Karaa (2016) considered duration dependency and tried to realize relevant bull and bear markets notions. Fukuta and Yamane (2015) compared the performance of equity duration with Capital Asset Pricing model and Fama–French model in the Japanese stock market. Project Duration has been defined to be consistent with the following:

$$\text{Project Duration} = \frac{\sum_{t=1}^{n} \frac{CF_t}{(1+r)^t}(t)}{\sum_{t=1}^{n} \frac{CF_t}{(1+r)^t}} \quad (1)$$

where: t—cash flow number in time t; CF—cash flow amount; n—period number; r—discount rate of the project.

Project Duration is in fact a combination of a project's time, cost, and return measures, which are defined in an index. The unit of this measure is time and therefore this is an index with a time unit. Project Duration is a measure of how long it takes for the present value of the future returns to fully repay the present value of future costs of the project. It should be noted that Duration can be very different from the project's period or life cycle. It is in fact the time and the amount of costs and returns of the project, as well as the discount rate that determines it. If the earnings of a project start earlier, or a big part of its costs are at the later phases of the project's life cycle, then the Duration of that project will be less compared to similar projects. The Duration of the project can provide valuable information for portfolio and project managers; which may not available through other measures.

In the model, for project value creation, several elements must be considered which are presented in Figure 1.

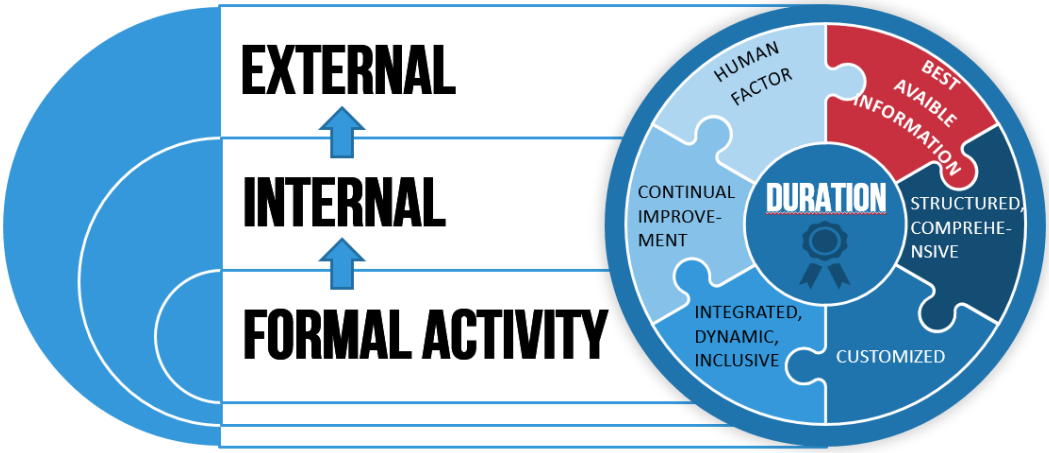


Figure 1. The elements for the project value creation.

The model for the value creation must include all types of risks. The risk can be assessed with a developed hybrid MCDM technique for risk management (Chatterjee et al. 2018). Ghasemi et al. (2018), Yousefi et al. (2018) presented project portfolio risk identification and analysis, considering project risk interactions and using Bayesian networks. Valipour et al. (2017) developed the hybrid SWARA-COPRAS method for risk assessment. Asadi et al. (2018) presented project risk evaluation by using a new fuzzy model based on the Elena guideline. Shariati et al. (2017) analyzed the critical factors by using the ANP technique under a fuzzy intuitionistic environment. The sustainable development criteria must all be integrated into the project value creation system (Hatefi and Tamošaitienė 2018).

Choosing an appropriate risk measure must be considered as well. Yousefi et al. (2018) investigated the impact made by the selection of various risk measures. In their research, semi-standard deviation was used to differentiate between desirable and undesirable opportunities. Value at Risk and Expected Shortfall were applied to make a better estimate of the tail risks. To explore this concept and its applications on different projects, we have used the Monte Carlo Simulation to compare its changes in different projects. The Monte Carlo approach has been applied a lot to deal with complex project management problems. The Monte-Carlo simulation is a possible solution for dealing with multi-dimensional problems, as indicated by Cong and Oosterlee (2016). Cesari and Cremonini (2003) compared the dynamic strategies of asset allocation by using this approach. Pajares and Lopez-Paredes (2011) used it to acquire the cost and time distribution at the end of the project (Acebes et al. 2015). Denault and Simonato (2017) applied simulations-and-regression for Dynamic portfolio selection. Cong and Oosterlee (2016) applied this method for a Multi-period mean–variance portfolio optimization. Brandt et al. (2005) used it in a dynamic portfolio selection, as did Denault and Simonato (2017). Wang et al. (2016) applied Monte Carlo for calculating the Value at Risk. (Buchner 2015) proposed the Monte Carlo method for Equilibrium option pricing. By assuming the stochastic nature of the projects' characteristics, Acebes et al. (2015), proposed to apply a statistical learning method and a Monte Carlo simulation. To conduct this research, several different projects of a construction company are grouped in similar categories, based on the experts' points of view and according to their time, cost, return and risk characteristics. Each of firm's new projects fall into one of the 15 defined groups, according to their unique characteristics. Then, according to the distributions of each of these projects and Monte Carlo simulation, the data were simulated 10,000 times and the cash flows of each project have been estimated. In the figures below, the overlay charts of Duration and NPV distributions for all groups of projects are illustrated in Figures 2 and 3.

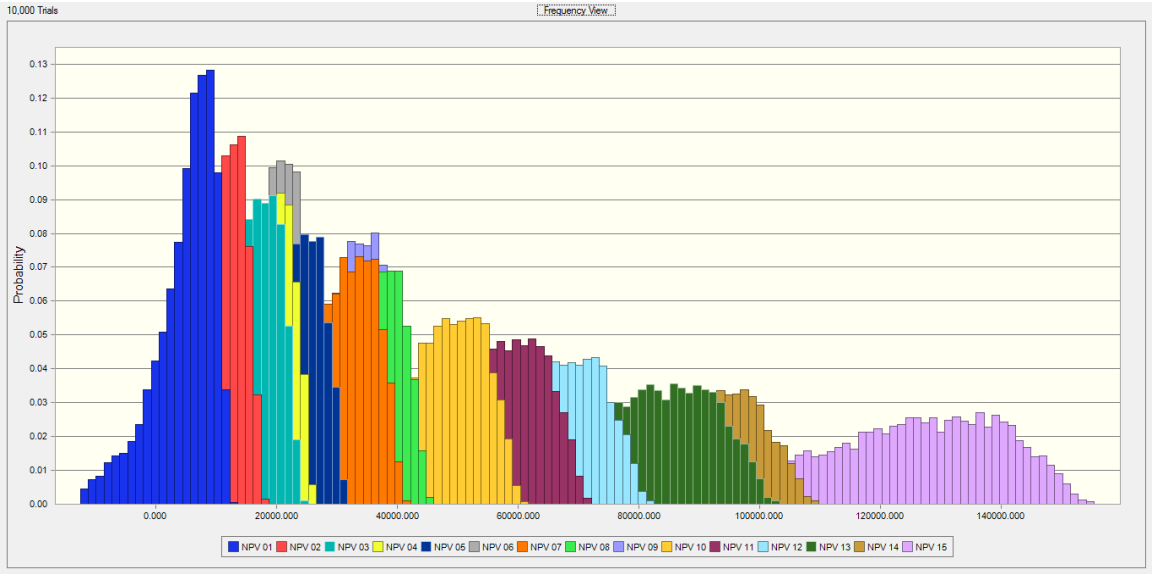


Figure 2. Overlay charts of NPV distributions.

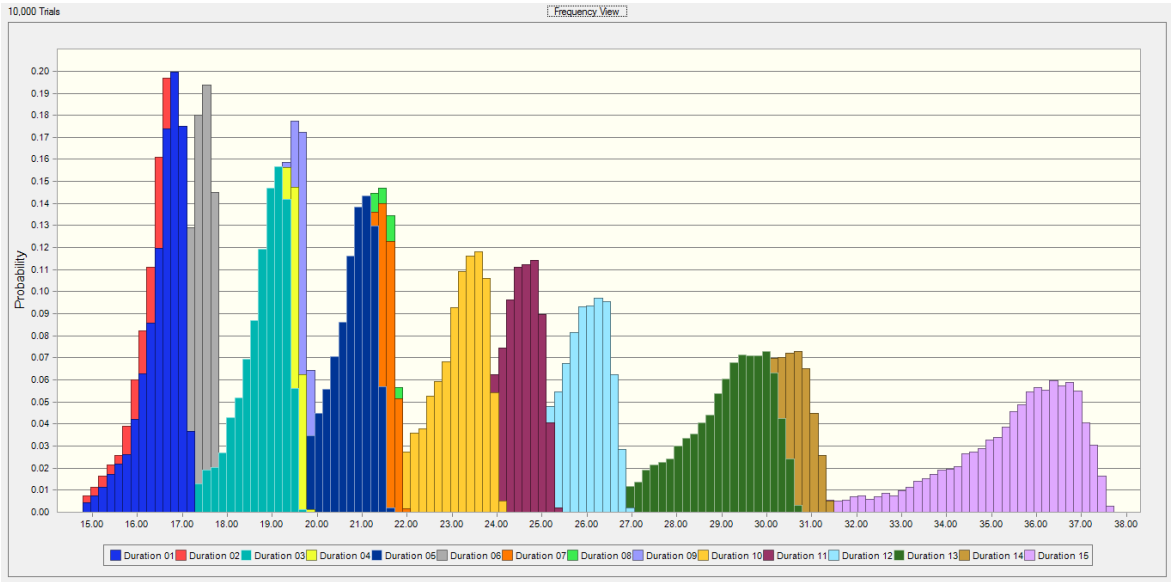


Figure 3. Overlay charts of Duration distributions.

At the later stages of this study, there has been an attempt to estimate the impact of changes on each of these measures, according to the shift in the discount rate. It should be noted that the minimum amount of possible discount rate is 0%. That is, the negative discount rate is not meaningful for projects. So, in a Monte Carlo simulation, the log-normal distribution has been used for the discount rate. In Figures 4 and 5 below, the effect of changes in NPV and Duration measures have been illustrated alongside the changes in the discount rate are presented.

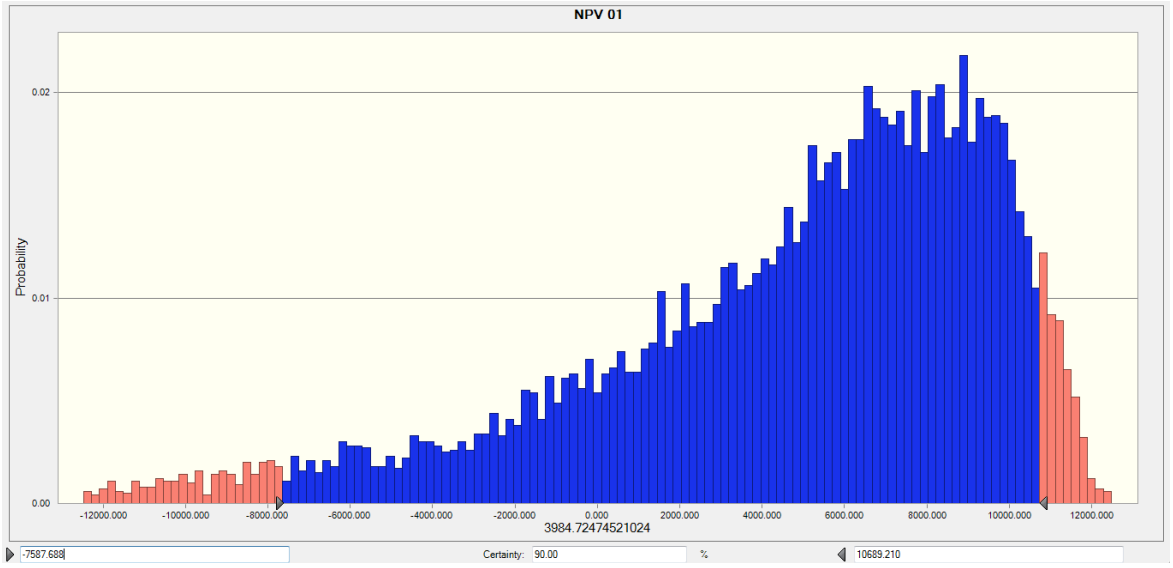


Figure 4. The NPV distribution with the changes in discount rate.

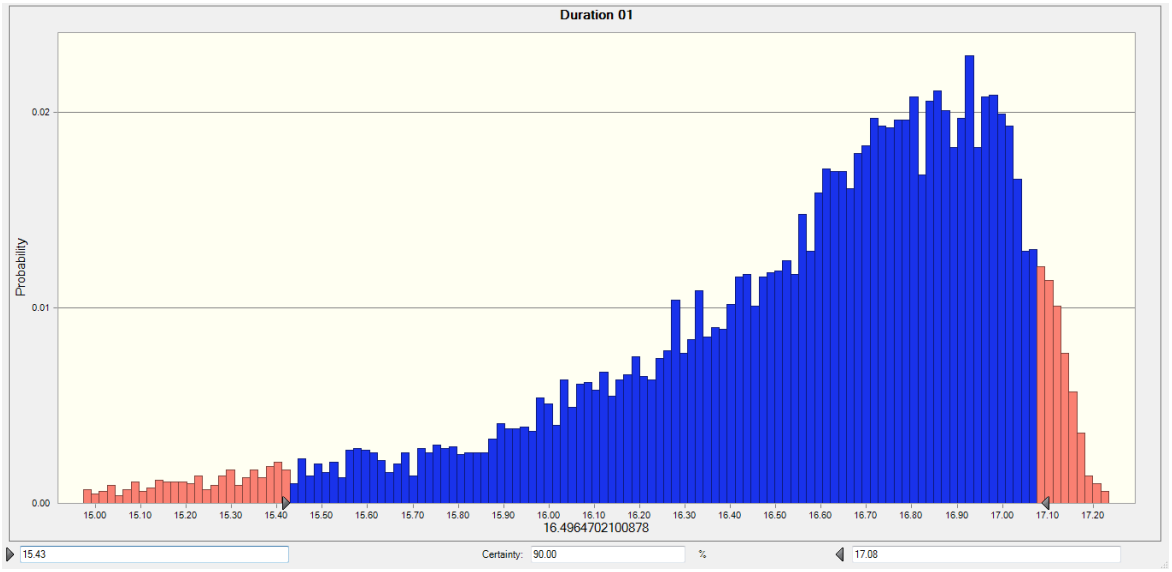


Figure 5. The Duration distribution with the changes in discount rate.

It is clear from the above figures that the NPV and Duration distributions of projects have negative skewness. Therefore, changes in the discount rate will lead to a non-normal distribution, wherein the possibility of occurrence of bad results (negative NPV) is more than the normal distribution.

3. Duration and Sensitivity of the Project Returns to Changes in Discount Rates

Another issue is the relationship between the changes in NPV and the discount rate. These two have an inverse relationship, meaning that, as expected, an increase in the discount rate will result in a decrease in a project's NPV. One application of the Duration measure could be the estimation of the NPV changes by changing the discount rate. It should be noted that one of the most important assumptions taken by managers in the feasibility study phase of the project is the assumption of the discount rate. Duration can provide management with an estimate of possible changes in NPV for the changes in the discount rate.

Much research has been conducted for choosing the appropriate discount rate of the projects. Lee and Lee (2017) proposed a method to predict the real discount rate. Jagannathan et al. (2016) concluded that firms use higher discount rates which are approximately twice the firms' capital cost. Firms apply these higher discount rates to account for idiosyncratic risks. Jouini and Napp (2014) discussed an equilibrium approach for the aggregation of discount rates. de Vasconcelos et al. (2016) examined the impact of various discount rates on refurbishment decisions of construction projects. Groom et al. (2007) in their paper show that the employment of models that account for changes in the interest rate generating mechanism has important implications for operationalizing a theory of DDRs that depends upon uncertainty.

In some research, the liaison of discount rates and time horizons was investigated. Hansson et al. (2016) studied this relationship on a long-term basis. Kossova and Sheluntcova (2016) studied the social discount rate in public sector projects in Russia, Kazlauskienė (2015) surveyed its application for assessment of public investment projects, and García-Gusano et al. (2016) discussed its role on energy systems optimization models. Nesticò and Maselli (2019) in their research considered the Social Discount Rate (SDR) in Cost-Benefit Analysis for making economic evaluations. This measure allows us to make the costs and the benefits that an investment generates over time financially comparable. This rate must reflect the organization and project's Weighted Average Cost of Capital (WACC), and also be consistent with the project's risk. Even for an organization with a constant weighted average cost of capital, the discount rate of two different projects must not be the same. The amount of this discount rate should be adjusted consistently with the project's risk, and of course, the amount of the risk in different phases of a project can change. The amount of an organization's risk

appetite and management's perception of risk are very effective in the appropriate allocation of discount rate as well. There are numerous assumptions in choosing appropriate discount rates. Thus, it is practical to have a measure that provides the management with a perspective on the influence of the changes in discount rates on the projects. Duration helps the project and portfolio managers to have an estimate of possible changes in NPV. In Figure 6 below, it is clear that there is a strong relationship between the NPV of the project and defined Duration.

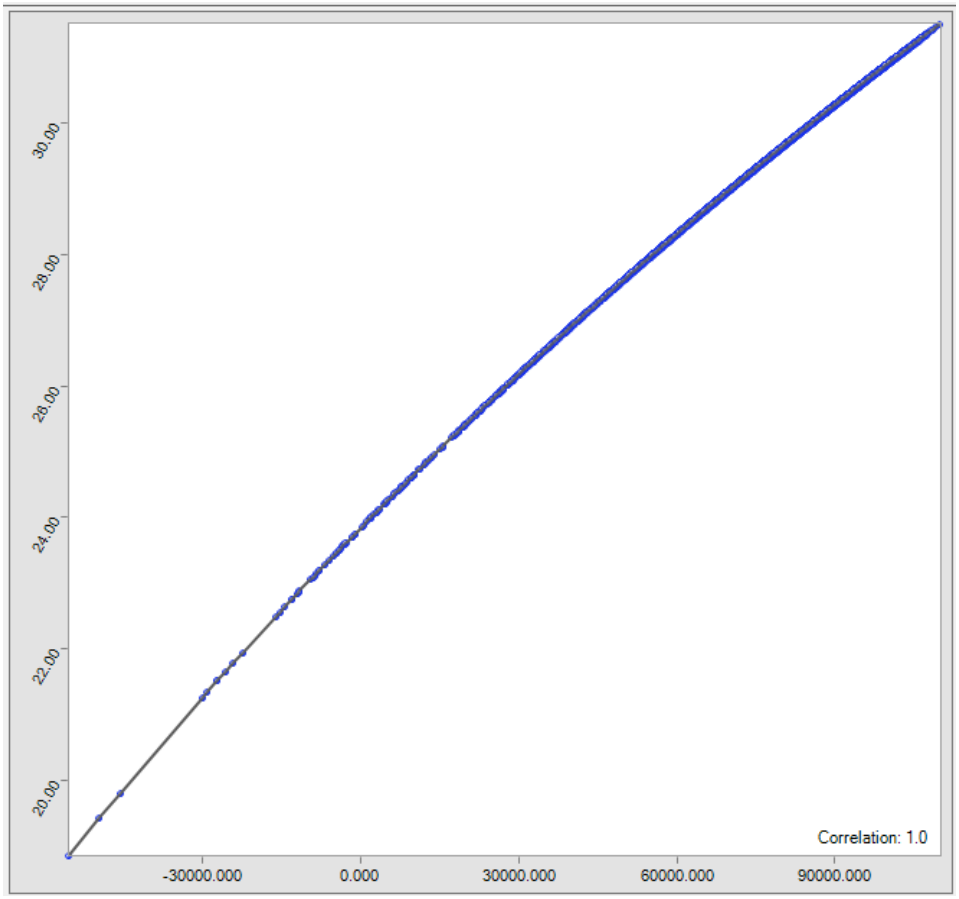


Figure 6. Correlation between the NPV of the project and defined Duration.

It should be noted that, projects with a higher duration have more risk and the volatility of their NPV is higher. Duration can be considered as a measure to estimate sensitivity of NPV to changes in discount rates. Since NPV is an important measure in selection of proper projects for the firm, and other indices in choosing projects are in some way related to NPV, it can be helpful to have a criterion for its sensitivity. In other words, projects with a higher duration have more sensitivity to changes in the discount rate and higher volatility in their NPV. Since projects' NPV are calculated according to the assumptions regarding the discount rate, management should not merely focus on the amount of NPV when choosing proper projects for the organization. The Duration measure can provide the manager with an index of NPV sensitivity. Therefore, if the managers are looking for appropriate projects for investment, they must select projects with the maximum NPV and minimum duration, which have less sensitivity with the assumptions of discount rate. A higher duration means more sensitivity and thus indicates projects with more volatility (higher risk). If the manager considers the assumptions regarding the discount rate as being conservative and decides to select projects with more volatility, which may contain proper opportunities, he should select the projects with a higher duration.

As was mentioned, duration reflects NPV's sensitivity to the assumptions regarding the discount rate, and it can be used to obtain an estimate of the future changes in NPV. As discussed, one of the applications of this new measure is to forecast the changes in the NPV by varying the

amount of discount rate. In Figure 7, the difference between forecasted changes with duration and actual NPV changes (error Term) have been illustrated for 1000 trials.

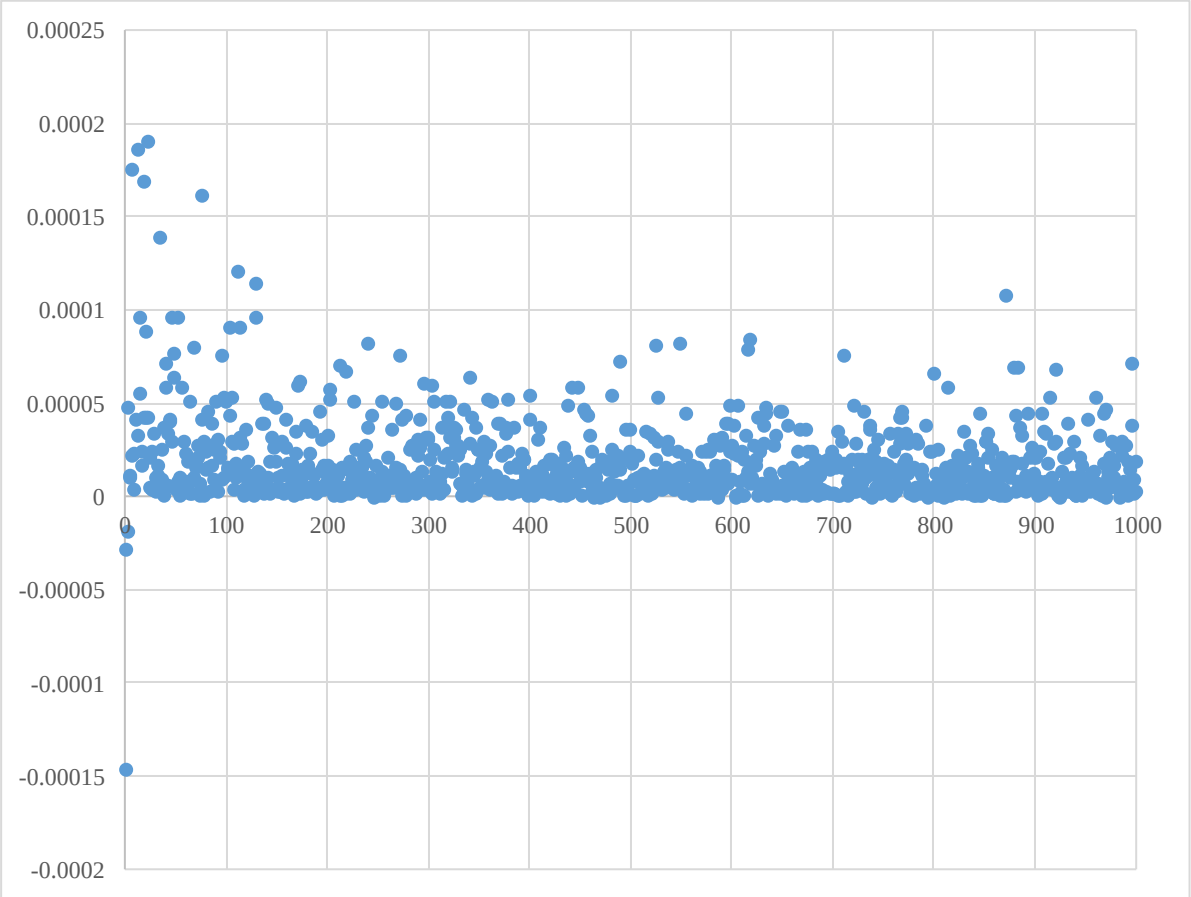


Figure 7. Error term diagram, difference between forecasted changes with duration and actual NPV changes.

It is necessary to note that the amount of duration may change with project execution. That is, by passing time, and with the payment of costs and receiving of project returns, the duration changes, which necessitates reassessment of it. Clearly, with the passage of time and the project progression, the amount of duration decreases. With every return received from the project, the amount of duration increases immediately and then it further decreases gradually by project progression. Therefore, the overall amount of duration is continually decreasing, with smaller sudden increases at the times of receiving the project returns.

4. Convexity

As is evident from Figure 7, the relationship of NPV with the changes in discount rate is a convex one. This convexity shows that for every one unit change of the discount rate in different rates, the amount of change in NPV can vary. The basic idea of the duration is to use the concepts of the duration and convexity for matching the price sensitivities of future and spot positions (Bessler and Wolff (2014); Kolb and Chiang (1981, 1982)). Osborne (2005) developed a more precise formula compared to adding convexity. Fricke and Menkhoff (2015) used a convexity adjustment term in their model. Shaffer (2007) estimated duration and convexity by considering risks of failure. Lesseig and Stock (2000) examined the duration and convexity of both senior and junior debt, and Sarkar (1999) did the same for zero-coupon convertible bonds. (Hanson 2014) studied the convexity effect in the mortgage backed securities (MBS) which have an embedded prepayment option. Gupta and Subrahmanyam (2000) investigated convexity bias in the pricing of interest rate swaps. Hyong-Chol et al. (2016) considered the convexity of stock price and exercise price relationship in Black–Scholes

equations. Houweling et al. (2005), Lu et al. (2017) also considered the positive convexity effect and concluded that the loss of market value of downgraded bonds in a high-interest-rate environment is less than that of a low-interest-rate environment. Grieves et al. (2010) examined and determined whether contract prices display negative convexity. It is clear that the amount of NPV changes by considering various discount rates. As expected, the NPV declines by increasing the expected discount rates. In the following table the amount of change in the NPV is shown for different discount rates and it is clear that this change is not linear. As mentioned, one of the purposes of defining duration is to use it for prediction of this change and if this relationship is not linear the amount of errors of the forecast can be non-negligible. Figure 8 shows the amount of this convexity that we want to estimate.

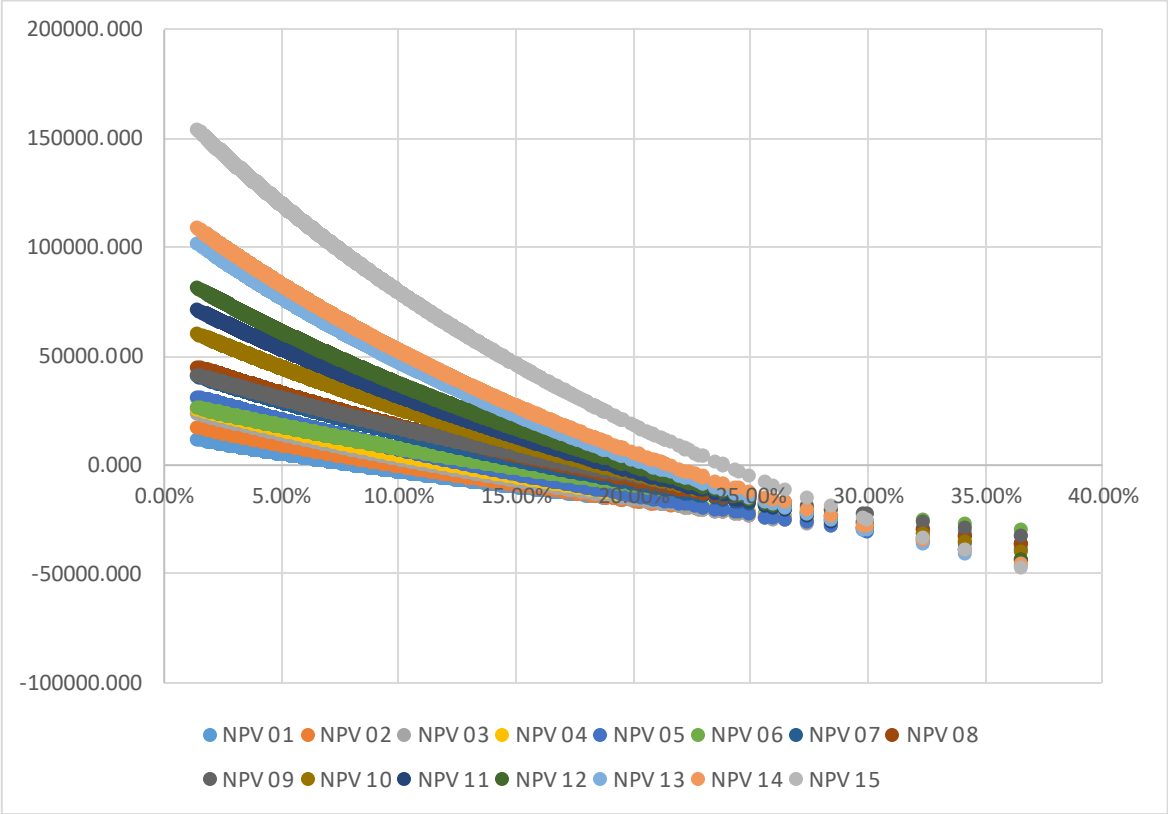


Figure 8. The amount of NPV changes in different discount rates.

The important intuition from this chart is the difference in the changes of NPV for every unit of increase or decrease in the discount rate. In the table below, the amount of change in NPV has been determined for one percent increase and decrease in the discount rate are presented in the Table 1.

Table 1. The amount of change in NPV for one percent volatility in the discount rate.

Project	Discount Rates									
	2.00%	1 Unit Decrease 1.00%		1 Unit Increase 3.00%		5.00%	1 Unit Decrease 4.00%		1 Unit Increase 6.00%	
	NPV	NPV	Percentage Change in NPV	NPV	Percentage Change in NPV	NPV	NPV	Percentage Change in NPV	NPV	Percentage Change in NPV
1	11,122	13,034	17.19	9263	−16.71	5696	7455	30.88	3985	−30.05
2	16,346	18,640	14.03	14,116	−13.64	9836	11,947	21.45	7783	−20.88
3	22,481	25,199	12.09	19,842	−11.74	14,791	17,280	16.83	12,373	−16.35
4	24,433	27,175	11.22	21,770	−10.90	16,670	19,183	15.08	14,227	−14.65
5	29,650	32,776	10.54	26,617	−10.23	20,817	23,674	13.72	18,043	−13.32
6	25,089	27,509	9.64	22,739	−9.37	18,235	20,455	12.18	16,076	−11.84
7	39,033	42,462	8.78	35,710	−8.51	29,364	32,489	10.64	26,333	−10.32
8	43,137	46,713	8.29	39,668	−8.04	33,029	36,300	9.90	29,853	−9.62
9	39,613	42,761	7.95	36,552	−7.73	30,679	33,575	9.44	27,860	−9.19
10	57,766	62,306	7.86	53,373	−7.60	45,002	49,121	9.15	41,013	−8.86
11	68,355	73,589	7.66	63,288	−7.41	53,630	58,382	8.86	49,026	−8.58
12	77,966	83,874	7.58	72,264	−7.31	61,443	66,759	8.65	56,307	−8.36
13	97,834	105,263	7.59	90,696	−7.30	77,239	83,836	8.54	70,893	−8.22
14	104,350	112,017	7.35	96,983	−7.06	83,088	89,900	8.20	76,533	−7.89
15	148,149	158,358	6.89	138,350	−6.61	119,903	128,941	7.54	111,217	−7.24

As it is evident from the table and can be perceived from the convexity of the diagram, in every discount rate, the amount of increase in NPV for one percent decrease in discount rate is more than the amount of decrease in NPV for one percent increase in the discount rate. This difference is shown in the table above. Moreover, in higher discount rates, the amount of changes in the NPV of a project is much more than that of low discount rates. It should be noted that the discount rate of any project is determined according to the weighted average cost of capital of the organization/project, as well as the risk. Therefore, it can be concluded that using projects with less risk and also low a duration, will lead to lower volatility of NPV. It also reflects the importance of an organization/project's financing to be able to lower the weighted average cost of capital. Various financing methods have different capital costs, which, as it is evident, have great impact on the final result of the project and its returns. The importance of this effect is even greater in higher discount rates. That is, the method of financing is more important for high-risk projects, than it is for low-risk ones. As is evident, the importance of this financing is even more influential in high rates than project cost management. That is the case while sometimes all of the efforts of management are put into lowering the costs, even though the focus should be directed towards lowering the risk of the project and its cost of capital. That is because lowering the project risk can substantially help lower its financial costs.

This, once more, shows the importance of risk management for lowering the project risks and the effort to lower the cost of capital. If successful, the benefits of this improvement are greater than a situation in which the said effort has failed and has led into an increase in risk and cost of capital. It can also be useful to consider that, in practice, one percent decrease in the discount rate will be much more feasible in higher rates than it is in lower rates. That is, changes that can be made to lower the risk or cost of capital, at high rates, are more probable. However, the benefits of lowering this rate at high discount rates, are greater. This emphasizes the importance of risk management and proper financing of projects.

5. Discount Rate Risk and Reinvestment Risk

Companies and projects have different financing methods, based on maturity, the type of organization, the type of projects, the country of origin and many other factors. Based on the source of financing (equity, debt and etc.) and their proportions, the company's capital costs change. This cost of capital affects the discount rate of organization's projects. The risk of the project affects the discount rate, as well. That is, all of the projects of one firm (which may even have the same cost of capital for all the projects) do not have the same discount rate and the company adjusts the discount rate of each project, based on its unique risks. Projects may have numerous risks. The effects of most of these risks can be considered using the proper discount rate. Since duration displays the NPV's sensitivity according to the changes in the discount rate, it can represent the discount rate risk. Therefore, projects with higher duration have higher sensitivity to this discount rate risk. The higher the project duration is, the more the firm has to wait to earn back the funds invested in that project. As was mentioned before, the greater duration means more volatility in project return. On the other hand, projects with higher returns (higher NPV and IRR) have a lower duration, because projects with higher return repay their costs sooner. Moreover, shorter time intervals for project earnings result in a lower project duration.

Based on the presented definition of project duration, it is equal to the time it takes to present the value of project costs to be repaid. Therefore, in that time, the organization can start another project. However, if there is no possibility for starting a proper new project or the conditions have changed in a way so that the organization can start a similar project with lower return or higher risk (and therefore a higher discount rate), then reinvestment risk exists. Projects with a lower duration have a higher reinvestment risk. Therefore, the management must select the project with the appropriate duration, according to the current macroeconomic and organizational conditions, and predictions of the future. This selection should have the proper level of both risks based on the situations. It should be noted that an inverse relationship exists between these two risks and with a decrease in the discount rate risk, the reinvestment risk increases. Choosing the proper level of these risks require optimization.

Selection of the appropriate project duration is closely correlated to organization and project's finance method. If a big part of discount rate of the project is allocated based on the weighted average cost of capital of the organization and the project, then a smaller part of the discount rate will be influenced by the project risk. So, if the finance method of the organization can keep the cost of capital fixed, the marginal change of the discount rate decreases. Therefore, the discount rate volatility, and as a result the return volatility decreases. Under these conditions, if the manager forecasts that the capital costs will increase in the future, he must select projects with a higher duration to minimize the reinvestment risk. That is because execution of a similar project in the future will entail a higher cost of capital and higher discount rate and therefore, a lower expected return. In this situation, selection of a project with a higher duration will improve organizational benefits and gains. Thus, optimization of duration and considering it in selecting projects can lead into an increase in the portfolio and the organization's value. This can be helpful in selecting appropriate projects for the organization. One of the applications of duration can be the optimization of firm's project portfolio, with the duration as a constraint. Also, duration can provide management with an estimate of the appropriate starting time for new projects, because in fact, duration is the time it takes to receive present value of project costs. Therefore, the organization will have enough resources to start a similar project.

Another benefit of using duration is the selection of proper investment projects, based on the firm's balance sheet. A number of investment companies, such as pension funds and endowments have long-term liabilities. These organizations can invest in projects with a higher duration. Even though the discount rate risk in this type of projects is higher, they also have higher returns. Therefore, these companies can gain higher returns, based on their long-term liabilities. Therefore, duration can also be an appropriate criterion for the selection of an organization's projects. Optimization of this method can be similar to Asset-Liability Management (ALM) in finance and projects must be matched with their corresponding liabilities.

6. Conclusions

In the first step of this study, the projects were grouped according to their unique characteristics. Then, a Monte Carlo Simulation was used to estimate project's return and risks, with different discount rates. In this research, a new concept in project management literature, Duration, was defined. Duration has a long history and major applications in finance literature. All three concepts of return, cost, and time of the project were considered in the definition of Duration, and thus, the management can possess an index combined of a number of important project factors, using this measure.

Duration reflects the sensitivity of NPV and its volatility to changes in the discount rate. Therefore, the management can have a measure of NPV's volatility based on the assumptions. If the manager is willing to select projects with lower risk, or if he is uncertain of propriety of the discount rate, projects with a lower duration should be chosen. Furthermore, the duration of each project will provide the management with an estimate of the changes in NPV, if the discount rate is unreliable.

In this research, the convexity effects between NPV and discount rate have been examined. That is, the changes in NPV, with the changes in the assumptions of discount rate, are much higher in lower rates than they are in higher rates. Furthermore, the amount of change in NPV for each unit of increase or decrease in the discount rate also varies. This means that the benefits of the project from a decrease in the discount rate are greater than the losses realized by an increase in the discount rate of the same value. This shows the importance of special attention and investment in proper risk management systems to lower the risk and also appropriate project financing, because it has a great impact on the final result and return of the project.

A decrease in duration means a decrease in the discount rate risk, and an increase in the reinvestment risk. Since by the time respective to the duration of the project, the present value of its construction costs has been repaid, the company can then start another project. In the absence of suitable projects, or a change in the investment criteria, the start of a new appropriate project may not be possible, and the manager faces reinvestment risk.

Duration can be an appropriate criterion for selecting projects by investment companies. To this end, an approach, similar to Asset-Liability Management (ALM) approach in finance, can be used and projects that match the liabilities periods can be selected. The benefits of using this method are much greater than the conservative method of simple cash flow matching.

Author Contributions: V.Y. designed the research, set the objectives, studied the literature, analyzed data, designed and developed the model. J.T. and S.H.Y. gathered and analyzed the data, provided extensive advice throughout the study, revised the manuscript, methodology and findings, and provided extensive advice on the literature review, model development and its evaluation. Conceptualization, V.Y.; Methodology, V.Y.; Software, V.Y.; Validation, V.Y. and J.T.; Formal Analysis, V.Y.; Investigation, V.Y.; Resources, V.Y., S.H.Y. and J.T.; Data Curation, V.Y., S.H.Y. and J.T.; Writing-Original Draft Preparation, V.Y. and J.T.; Writing-Review & Editing, J.T. and S.H.Y.; Visualization, V.Y. and J.T.; Supervision, J.T. and S.H.Y.; Project Administration, V.Y., S.H.Y. and J.T. All authors discussed the model evaluation results and commented on the paper.

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